

Differential eq'n of mass transfer

o.s.s. o. no reaction in the diffusion domain.

$$\vec{\nabla} \cdot \vec{N}_A + \frac{\partial C_A}{\partial t} - R_A = 0$$

$$\Rightarrow \vec{\nabla} \cdot \vec{N}_A = 0$$

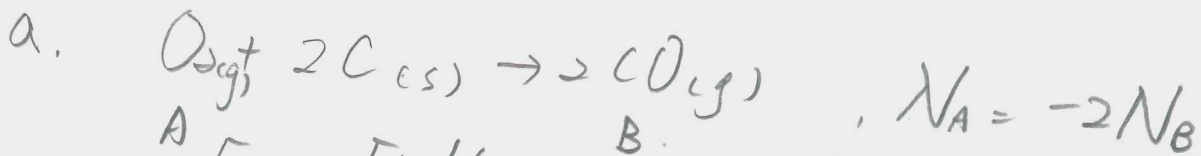
$$\Rightarrow \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 N_{A,r}) + \frac{1}{r \sin \theta} \frac{\partial}{\partial \theta} (N_{A,\theta} \sin \theta) + \frac{1}{r \sin \theta} \frac{\partial N_{A,\phi}}{\partial \phi} = 0$$

for mass flux in r direction only  $\Rightarrow N_{A,\theta} = N_{A,\phi} = 0$

$$\Rightarrow \frac{1}{r^2} \frac{\partial}{\partial r} (r^2 N_{A,r}) = 0$$

$$\Rightarrow \frac{\partial}{\partial r} (r^2 N_{A,r}) = 0$$

$\Rightarrow r^2 N_{A,r}$  is not a function of r in diffusion domain.



From Fick's 1st eq'n

$$\vec{N}_A = -CD_{AB} \vec{\nabla} y_A + y_A \sum_{i=1}^n \vec{N}_i$$

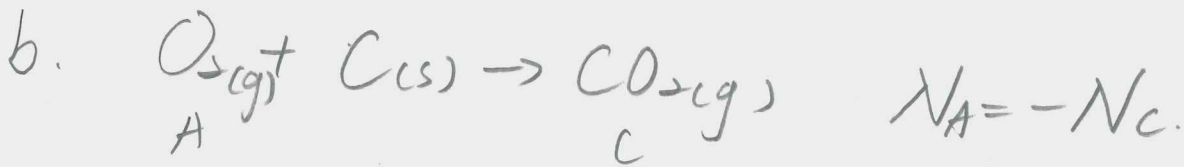
$$= -CD_{AB} \vec{\nabla} y_A + y_A (\vec{N}_A + \vec{N}_B)$$

for mass flux in r direction only, &  $N_{A,r} = -2N_{B,r}$

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$$N_{A,r} = -CD_{AB} \frac{\partial y_A}{\partial r} + y_A (-N_{A,r})$$

$$\Rightarrow N_{A,r} = \frac{-CD_{AB} \frac{\partial y_A}{\partial r}}{1+y_A}$$

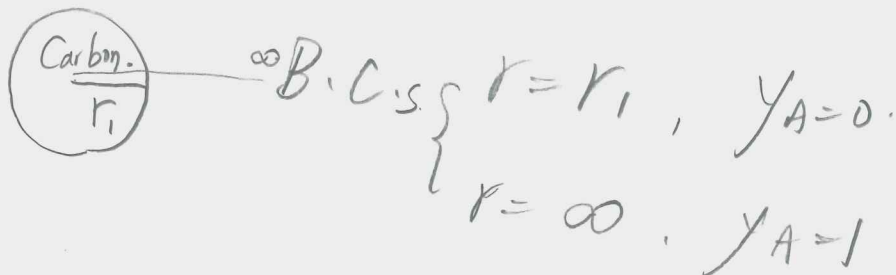


$$\vec{N}_A = -CD_{AC} \vec{\nabla} y_A + y_A (\vec{N}_A + \vec{N}_C)$$

mass flux in r direction only &  $N_{A,r} = -N_{C,r}$

$$\Rightarrow N_{A,r} = -CD_{AC} \frac{\partial y_A}{\partial r}$$

for reaction at the surface is instantaneous,  
the radius of carbon is constant



$$\alpha' \quad \text{O}_2 + 2\text{C} \rightarrow 2\text{CO}$$
$$N_{A,r} = -CD_{AB} \frac{\partial y_A}{\partial r} + y_A(-N_{A,r})$$

補充 (3)

$$\Rightarrow (1+y_A) N_{A,r} = -CD_{AB} \frac{\partial y_A}{\partial r}$$

$$\Rightarrow N_{A,r} dr = -\frac{CD_{AB}}{1+y_A} dy_A$$

$$\Rightarrow r^2 N_{A,r} \frac{1}{r^2} dr = -\frac{CD_{AB}}{1+y_A} dy_A$$

$$\Rightarrow \int_{r_1}^{r_2} \underbrace{r^2 N_{A,r}}_{\text{constant}} \frac{1}{r^2} dr = \int_{y_{A1}}^{y_{A2}} -\frac{CD_{AB}}{1+y_A} dy_A$$

$$\Rightarrow r^2 N_{A,r} \left( \frac{1}{r_2} - \frac{1}{r_1} \right) = -CD_{AB} \ln \left( \frac{1+y_{A2}}{1+y_{A1}} \right)$$

$$\Rightarrow N_{A,r} = \frac{1}{r^2} \frac{CD_{AB} \ln \left( \frac{1+y_{A2}}{1+y_{A1}} \right)}{\frac{1}{r_2} - \frac{1}{r_1}}$$