

Quiz 4.

1. a. see H.W. 4

b. $\frac{dc^*}{dt} = -k^* c^{*3}$, at $t=0$ $c^* = c_0^*$

$$\Rightarrow \frac{dc^*}{c^{*3}} = -k^* dt \Rightarrow -\frac{1}{2} c^{*-2} \Big|_{c_0^*}^{c^*} = -k^* \Big|_0^t$$

$$\Rightarrow -\frac{1}{2} \left(\frac{1}{c^{*2}} - \frac{1}{c_0^{*2}} \right) = -kt$$

$$\Rightarrow \frac{1}{c^{*2}} = \frac{1}{c_0^{*2}} + 2kt = \frac{1 + 2kt c_0^{*2}}{c_0^{*2}}$$

$$\Rightarrow c^* = \left(\frac{c_0^{*2}}{1 + 2k c_0^{*2} t} \right)^{1/2}$$

$$r_p = -\frac{1}{m_{cat}} \frac{dM}{dt} = k_p c^* k M$$

$$\Rightarrow \frac{dM}{M} = -m_{cat} k_p k c_0^* (1 + 2k c_0^{*2} t)^{-1/2} dt, \text{ at } t=0, M=M_0$$

$$\Rightarrow \ln \frac{M}{M_0} = -m_{cat} k_p k c_0^* \frac{(1 + 2k c_0^{*2} t)^{1/2}}{k c_0^{*2}} = -m_{cat} \frac{k_p}{c_0^*} (1 + 2k c_0^{*2} t)^{1/2}$$

$$\Rightarrow X = \frac{M_0 - M}{M_0} = 1 - \frac{M}{M_0} = 1 - \exp \left(-m_{cat} \frac{k_p}{c_0^*} (1 + 2k c_0^{*2} t)^{1/2} \right)$$

2. see class notes